# HIV-1 Capsid Function Is Regulated by Dynamics: Quantitative Atomic-Resolution Insights by Integrating Magic-Angle-Spinning NMR, QM/MM, and MD 

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## (S) Supporting Information


#### Abstract

HIV-1 CA capsid protein possesses intrinsic conformational flexibility, which is essential for its assembly into conical capsids and interactions with host factors. CA is dynamic in the assembled capsid, and residues in functionally important regions of the protein undergo motions spanning many decades of time scales. Chemical shift anisotropy (CSA) tensors, recorded in magic-angle-spinning NMR experiments, provide direct residue-specific probes of motions on nano- to microsecond time scales. We combined NMR, MD, and density-functional-theory calculations, to gain quantitative  understanding of internal backbone dynamics in CA assemblies, and we found that the dynamically averaged ${ }^{15} \mathrm{~N}$ CSA tensors calculated by this joined protocol are in remarkable agreement with experiment. Thus, quantitative atomic-level understanding of the relationships between CSA tensors, local backbone structure, and motions in CA assemblies is achieved, demonstrating the power of integrating NMR experimental data and theory for characterizing atomic-resolution dynamics in biological systems.


## INTRODUCTION

HIV-1 capsids, assembled from $\sim 1,500$ copies of the capsid (CA) protein, are an internal part of mature virions (Figure 1). ${ }^{1,2}$ Conical in shape, capsids enclose the viral genome together with several proteins that are essential for viral replication. ${ }^{3}$ During HIV-1 entry, intact capsids are released into the cytoplasm of the host cell, followed by disassembly (uncoating), which takes place in a tightly orchestrated fashion. The net result of these events is the integration of the reverse transcribed viral DNA into the host genome, necessary for viral replication. ${ }^{4,5}$

Capsids are pleomorphic, comprised of a varied number of copies of CA protein structural blocks, with variable curvature in the capsid shell and overall appearance. Pleomorphism is directly related to the conformational plasticity of the CA protein. ${ }^{7}$ Remarkably, in the assembled state, CA is dynamic over a range of time scales from nano- to milliseconds. ${ }^{6,8-10}$ Specifically, motions in the linker, which connects the CA's Nand C-terminal domains (NTD and CTD), occur on the milliseconds time scale and are directly linked to the capsid's

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Figure 1. (a) All-atom model of mature HIV-1 capsid determined by an integrated cryo-ET, solution NMR, and MD approach (PDBID: $3 \mathrm{~J} 3 \mathrm{Y}^{6}$ ). Hexameric (predominant) and pentameric (minor) building blocks are shown in blue and red, respectively. (b) Hexamer of hexamers $(\mathrm{HOH})$, a predominant structural element of the capsid. (c) 3D structure of an HIV-1 CA monomer (PDB file 3NTE). (d) Illustration of a backbone ${ }^{15} \mathrm{~N}^{\mathrm{H}}$ CSA tensor and its orientation in the protein molecular frame. (e) Transmission electron microscopy (TEM) image of tubular assemblies of CA HXB2. (f) A 2D NCA spectrum of tubular assemblies of $\mathrm{U}-{ }^{13} \mathrm{C},{ }^{15} \mathrm{~N} \mathrm{CA}$, recorded at 21.1 T and the MAS frequency of 14 kHz .
ability to assemble into varied morphologies. ${ }^{8}$ These motions, coupled with pH -dependent electrostatic interactions, may contribute to assembly control, involving a molecular switch. ${ }^{8}$

In the host cells, capsid interacts with host proteins. These interactions can either facilitate or inhibit the HIV-1 replication. One such protein is Cyclophilin A (CypA), which is required for the virus to be active in certain cell types. ${ }^{1,12}$ CypA interacts with the capsid by binding to the CypA loop located in CA's NTD, and mutants in the CypA loop can escape from CypA dependence. For instance, the A92E and G94D CA escape mutants are fully infectious when CypA/CA interactions are inhibited, while in the presence of CypA these mutants retain only $\sim 10 \%$ of infectivity. It has been proposed that CypA plays a role in stabilizing the capsid through a novel binding interface, where one CypA molecule bridges two CA hexamers, along the highest-curvature direction. ${ }^{13}$

CA/CypA interactions modulate capsid dynamics, and the virus takes advantage of this effect to escape from the CypA dependence. Specifically, CypA binding attenuates the motions of the CypA loop and also induces allosteric conformational changes in other regions of the protein. Remarkably, the dynamic behavior of A92E and the G94D CA mutants closely resembles that of the CA/CypA assembly, and the dynamic allosteric regulation mechanism was proposed to explain the capsid's escape from CypA dependence. ${ }^{10}$

The internal dynamics of CA also play a role in HIV-1 maturation. Initially, during virus budding from the host cell, the Gag polyprotein, which contains the main structural proteins of HIV (MA, CA, MA, NC, and p6), is a single polypeptide chain. During maturation, Gag is proteolytically cleaved into the individual domains by the HIV protease in an orderly, stepwise fashion. The final step is the cleavage of a 14residue spacer peptide 1 (SP1) from the CA-SP1 maturation intermediate to release CA, which, in turn, organizes into the conical cores characteristic of mature virions. In CA-SP1, the SP1 peptide is highly flexible and its presence affects the mobility of distal residues, such as those in the CypA loop. ${ }^{14}$ Clearly, dynamic regulation is an important ingredient in the final maturation step, and the above-described studies highlight the importance of understanding residue-specific conformational dynamics in HIV-1 capsid assemblies, given the direct relationship between dynamics and virus function.

Previously, we analyzed ${ }^{1} \mathrm{H}-{ }^{15} \mathrm{~N} /{ }^{1} \mathrm{H}-{ }^{13} \mathrm{C} /{ }^{15} \mathrm{~N}-{ }^{13} \mathrm{C}$ dipolar interactions as well as resonance intensities and line widths, demonstrating the power of combining MAS NMR and MD simulations for determining the motional modes of the individual residues. Here, we focus on ${ }^{15} \mathrm{~N}$ chemical shift anisotropy (CSA) tensors as sensitive probes of nano- to microsecond dynamics in HIV-1 capsid assemblies. We integrate quantum mechanics/molecular mechanics (QM/ MM) calculations of magnetic shielding anisotropy, using density functional theory (DFT), with MD simulations and MAS NMR to gain quantitative insights into the effects of dynamic averaging on CSA tensors. We show that the experimental and calculated ${ }^{15} \mathrm{~N}$ CSA tensors are in remarkable agreement, including those for dynamic residues, such as in the CypA-binding loop, and that dynamic averaging of chemical shifts has to be taken into account. The integrated approach described here is broadly applicable to any system and is particularly important in NMR-based structure determination of dynamic regions in protein assemblies.

## RESULTS AND DISCUSSION

Experimental NMR Parameters. Tubular assemblies of HIV-1 CA yield highly resolved MAS NMR spectra (Figure 1), and they permitted assignments of ${ }^{13} \mathrm{C}^{\alpha},{ }^{13} \mathrm{C}^{0}$ and ${ }^{15} \mathrm{~N}$ chemical shifts for 222,188 , and 210 residues, respectively. Backbone ${ }^{15} \mathrm{~N}$ CSA tensors for individual residues were derived from a 3D R14 ${ }_{2}{ }^{5}$-symmetry based RNCSA experiment. ${ }^{15,16}$ The experimental ${ }^{15} \mathrm{~N},{ }^{13} \mathrm{C}^{\alpha}$, and ${ }^{13} \mathrm{C}^{0}$ isotropic chemical shifts, $\delta_{\text {iso }}$, are plotted vs residue number in Figures 2 and 3, and reduced anisotropy parameters are plotted in Figure 3d as well as CSA line shapes being shown in Figure 3 e and Figure S1 (Supporting Information).

It is well-known from solution NMR studies that isotropic chemical shifts are modulated by dynamics, ${ }^{17}$ and MD simulations in conjunction with empirical ShiftX-based calculations were reported to explain the dynamic averaging of $\delta_{\text {iso }}$ in RNaseH. ${ }^{18}$ Here, for CA assemblies, large variation in ${ }^{15} \mathrm{~N},{ }^{13} \mathrm{C}^{\alpha}$, and ${ }^{13} \mathrm{C}^{0} \delta_{\text {iso }}$ is seen for the different residues, and the extent of variability is generally greater for the loop vs the helical regions of CA (Figure S2, Supporting Information). However, no obvious trends that would suggest the presence of motions in specific regions of the protein can be noted. In contrast, the experimental reduced anisotropy parameters of the ${ }^{15} \mathrm{~N}$ CSA tensors, $\delta_{\sigma}$, are dramatically different along the CA sequence; see Figure 3d. Most notably, the residues in the


Figure 2. Backbone isotropic chemical shift parameters in tubular assemblies of CA, plotted as a function of the residue number: (a) ${ }^{13} \mathrm{C}^{\alpha} \delta_{\text {iso }}$ and (b) ${ }^{13} \mathrm{C}^{\mathrm{O}} \delta_{\text {iso }}$. The parameters are shown as follows: isotropic chemical shifts recorded from NMR experiments, black; calculated by MD/DFT, red; calculated by DFT from a single X-ray structure, blue; calculated by ShiftX, orange. The gray rectangles denote the loop regions of the CA protein.

CypA loop exhibit low $\delta_{\sigma}$ values for A88, G89, A92, and G94 of $50.4,40.3,70.9$, and 59.0 ppm , respectively (the corresponding rigid-limit values are 96.0, 95.3 , 102.6, and 92.8 ppm , based on a DFT calculation using the X-ray structure geometry; PDBID: 3NTE). While it is known that differences in the secondary structure and local interactions (hydrogen bonding and solvent interactions) affect the ${ }^{15} \mathrm{~N}$ CSA tensors in proteins, ${ }^{19,20}$ the dramatic reduction of $\delta_{\sigma}$ observed for the residues in the CypA loop residues, compared to the rigid value limits, cannot be explained by a structural effect alone. Greatly attenuated $\delta_{\sigma}$ values were also observed for several other residues, primarily in the loop regions of both the NTD and CTD.

We previously demonstrated via a combined MAS NMR and MD simulations approach, using ${ }^{1} \mathrm{H}-{ }^{15} \mathrm{~N} /{ }^{13} \mathrm{C}^{\alpha}$ dipolar tensors, that residues in loop regions are mobile, with those in the CypA loop unusually flexible on the nano- to microseconds time scale. ${ }^{10}$ Therefore, we hypothesized that these internal motions may cause partial averaging of the backbone CSA tensors, similar to the dynamic effects on CSA tensors observed in other proteins. ${ }^{21,22}$ This notion was examined in the present study.

Understanding the Mechanism of Dynamic CSA Averaging by Integrating NMR, MD, and QM/MM Calculations. To test the hypothesis that dynamics influence CSA tensors in CA assemblies in a major way, we computed CSA tensors using a $\mathrm{QM} / \mathrm{MM}$ approach, with the quantum
region being treated at the DFT level. In parallel we also calculated isotropic shifts by ShiftX. ${ }^{23}$ These calculations were carried out for a monomer extracted from the CA X-ray structure (PDBID: 3NTE) as well as for individual CA substructures, using the reported 100 ns MD trajectories. ${ }^{10}$

As evidenced from the data in Figure 2 and Figure 3, the ShiftX-based predictions of isotropic chemical shifts agree well with the NMR experiments, because these calculations, by the nature of their database driven properties, take into account dynamic averaging of isotropic shifts for mobile regions, as reported previously by several groups. ${ }^{24-27}$ On the other hand, DFT-calculated values based on the CA X-ray structure are not in agreement with experiment, neither for the reduced anisotropy parameters nor for the isotropic shifts. For example, the experimental ${ }^{15} \mathrm{~N} \delta_{\sigma}$ vary over a large range, from 40.4 to 106.3 ppm , while the calculated ${ }^{15} \mathrm{~N} \delta_{\sigma}$ exhibit only small variations $(99.0 \pm 15.4 \mathrm{ppm})$. RMSD values from DFT calculations are $6.2,4.4$, and 12.6 ppm for ${ }^{15} \mathrm{~N} \delta_{\text {iso, }}{ }^{13} \mathrm{C} \delta_{\text {iso }}$, and ${ }^{15} \mathrm{~N} \delta_{\sigma}$, respectively. Furthermore, no correlation with secondary structure is seen and residues in the CypA-binding loop were not predicted to have uniquely attenuated anisotropy. Likewise, the calculated isotropic ${ }^{15} \mathrm{~N},{ }^{13} \mathrm{C}^{\alpha}$, and ${ }^{13} \mathrm{C}^{0}$ shifts do not reproduce the experimental parameters.

In contrast, the dynamically averaged ${ }^{15} \mathrm{~N}$ CSA tensors computed by MD/DFT are generally in remarkably good


Figure 3. Backbone ${ }^{15} \mathrm{~N}^{\mathrm{H}}$ chemical shift parameters in tubular assemblies of CA, plotted as a function of the residue number: $\delta_{\text {iso }}(\mathrm{a}-\mathrm{c})$ and $\delta_{\sigma}(\mathrm{d})$. The parameters are shown as follows: isotropic chemical shifts or reduced chemical shift anisotropy recorded from 3D RNCSA NMR experiments, black; calculated by MD/DFT, red; calculated by DFT from a single X-ray structure, blue; calculated by ShiftX, orange. The error bars are shown on the experimental $\delta_{\sigma}$ values. The gray rectangles denote the loop regions of CA protein. (e) Experimental (solid black lines) and simulated (dashed red lines) ${ }^{15} \mathrm{~N}^{\mathrm{H}}$ RNCSA line shapes plotted for selected CA residues; the best fit CSA parameters are indicated above each spectrum.
agreement with experiment, as shown in Figures 3 and 4. Importantly, the dramatic reduction in ${ }^{15} \mathrm{~N} \delta_{\sigma}$ values for the CypA-loop residues that was observed experimentally is captured in the computations, indicating that this decrease is caused by internal loop dynamics rather than by structural effects. This finding is consistent with our prior results from dipolar tensors. ${ }^{10}$ In addition, the extent of CSA averaging increases for the residues in the middle of the CypA loop, where the largest motional amplitudes and extensive sampling of conformational space is expected. ${ }^{10}$ An outlier in that regard is G89, for which the computational results suggest a considerably smaller ${ }^{15} \mathrm{~N} \delta_{\sigma}$ ( 23.75 ppm ) than the experimentally observed value ( 40.3 ppm ). While such a deviation in $\delta_{\sigma}$ values is generally considered to be acceptable for quantum mechanical calculations, it may also be the result of insufficient sampling, due to the length of the MD trajectory.

The overall agreement between the experimental and MD/ DFT computed $\delta_{\text {iso }}$ is poorer than that for $\delta_{\sigma}$; see Figures 2 and 3 and 4 e . Considerable scatter is noted, and the slope of 0.77 and offset of 21.6 ppm are significantly greater than those reported for previous DFT calculations of ${ }^{15} \mathrm{~N}$ chemical shifts for 20 structurally characterized proteins. ${ }^{28}$ To gain further insights into the effect of dynamic averaging on the ${ }^{15} \mathrm{~N}$ CSA tensors, we analyzed their experimental and computed principal components, $\delta_{11}, \delta_{22}$, and $\delta_{33}$. These are plotted vs the residue number in Figure $4 \mathrm{a}-\mathrm{c}$. The experimental and calculated $\delta_{\mathrm{ii}}$ correlate well; see Figure 4f: the slope is 0.98 , and a negligible
offset of -2.6 ppm is seen $\left(1.3 \%\right.$ of the entire range of $\delta_{\mathrm{ii}}$ values). The largest scatter for any principal component is observed for $\delta_{33}$ (Figure 4 c and 4 f ), suggesting that molecular motion affects most prominently the reorientation of the principal component perpendicular to the amide plane (Figure 1d). These results highlight the importance of measuring CSA tensors, not only isotropic shifts, for systems that possess internal dynamics.

Another interesting observation in this study relates to the finding that better agreement between the experiment and calculations is seen for NTD residues, compared to the CTD. This is evident from the data depicted in Figure 4, for both $\delta_{\text {iso }}$ and $\delta_{\sigma}$. We observed a similar effect in our studies of ${ }^{1} \mathrm{H}-{ }^{15} \mathrm{~N} /{ }^{13} \mathrm{C}^{\alpha}$ dipolar tensors, where alignments were carried out for the individual domains in the calculations in order to eliminate overall translational and rotational motions. ${ }^{10}$ The NTD and CTD are connected by a flexible linker, which is mobile on the slow-microsecond to millisecond time scales. ${ }^{8}$ CTD residues are more rigid according to the experimental CSA parameters than those computed by MD/QM/MM. Since $\mathrm{MD} / \mathrm{QM} / \mathrm{MM}$ calculations were conducted on monomeric CA, the intermolecular CTD-CTD interactions, which are essential for the capsid assembly and stability, ${ }^{6}$ could not be captured, rendering the CTD in the $\mathrm{MD} / \mathrm{QM} / \mathrm{MM}$ calculations more flexible than in tubular assemblies studied by MAS NMR.

To understand how the CSA tensors are affected by the reorientation of the corresponding residues during local


Figure 4. $(\mathrm{a}-\mathrm{c})$ Backbone ${ }^{15} \mathrm{~N}^{\mathrm{H}}$ principal components of the CSA tensors, $\delta_{\mathrm{ij}}$ in tubular assemblies of CA, plotted as a function of the residue number. The experimental values obtained from 3D RNCSA are shown in black; the values calculated by MD/DFT are in red. (d-i) The MD-DFT calculated CSA tensor parameters, $\delta_{\sigma}, \delta_{\mathrm{iso}}$, and $\delta_{\mathrm{i} i}$ plotted vs the corresponding experimental parameters. The parameters for both NTD and CTD are displayed in $(\mathrm{d}-\mathrm{f})$; those for NTD only are shown in $(\mathrm{g}-\mathrm{i})$.
motions, we examined the computed principal components of the ${ }^{15} \mathrm{~N}$ CSA tensors, $\delta_{\mathrm{ii}}$, and the isotropic shifts, $\delta_{\mathrm{iso}}$, for each residue along the MD trajectory. In Figure S3 (Supporting Information) we illustrated the results for two residues: G89 in the tip of the CypA-binding loop, which is highly mobile, and the more rigid E98. Interestingly, the variations in the principal CSA components are relatively modest, and independent of whether the corresponding residue is dynamic or static. However, as shown in Figure 5, for the dynamic G89, very large changes in the Euler angles $(\alpha, \beta, \gamma)$ are observed, associated with different orientations of the CSA tensors in the individual substructures in the MD trajectory. These kinds of motions are expected to attenuate the observed CSA tensors (see an illustration for a spin model in Figure S4 (Supporting Information). Conversely, for the static E98, these variations
are much smaller. The polar angles $\theta$, which relate each $\delta_{\mathrm{ii}}$ to the $\mathrm{N}-\mathrm{H}$ bond vector, on the other hand, are similar for both static and dynamic residues; see Figure 5. This indicates that motions exert larger effects on the relative orientations of the individual CSA tensors, while the individual principal components of the diagonal CSA tensor are affected less. This is vividly seen when the individual components of a nondiagonal CSA tensor, $\delta_{\mathrm{ij}}$ (where $\mathrm{i} / \mathrm{j}=\mathrm{x}, \mathrm{y}, \mathrm{z}$ ) are plotted in the molecular fixed frame (MFF) representation (Figure S5, Supporting Information), with variations predominantly being caused by the changing Euler angles. (MFF here coincides with the lab frame, since only one protein molecule is considered in calculations.) The dynamic averaging of the ${ }^{15} \mathrm{~N}$ CSA tensors is illustrated in Figure 6a-f for representative CypA-loop residues. The differences between mobile and rigid residues


Figure 5. (a) Amplitudes and orientations of backbone ${ }^{15} \mathrm{~N}^{\mathrm{H}}$ CSA tensors for G 89 (left) and E98 (right) in HIV-1 CA protein with respect to the molecular frame, for the individual structures along the MD trajectory at $t=0,1,2$, and 3 ns (from top to bottom, respectively). ( $\mathrm{b}-\mathrm{d}$ ) Plots of the relative angles between the principal components of the ${ }^{15} \mathrm{~N}$ CSA tensor, $\delta_{\mathrm{iij}}$, and the $\mathrm{N}-\mathrm{H}$ bond, $r_{\mathrm{N}-\mathrm{H}}$. (e-g) Euler angles for the backbone ${ }^{15} \mathrm{~N}^{\mathrm{H}}$ CSA tensors in the molecular frame. The CSA parameters and relative tensor orientations were calculated by QM/MM (at the DFT level) for the individual structures along the MD trajectory as a function of time, as shown for G89 (black triangles) and E98 (red circles).
are also apparent when comparing experimental $\delta_{\text {iso }}$ values with those computed by MD/DFT and MD/ShiftX (Figure S2, Supporting Information). Not surprisingly, loop residues that are mobile exhibit broad distributions, while residues in helices possess narrow chemical shift ranges. The corresponding residue-specific distributions computed by MD/ShiftX (Figure S6, Supporting Information) reveal that the width of the CS distribution correlates with the conformational space sampled by each residue in the course of the MD trajectory. This result
is consistent with our prior findings for dipolar tensors ${ }^{10}$ and with the solution-NMR studies of RNaseH. ${ }^{18}$

Given the computationally expensive nature of $\mathrm{QM} / \mathrm{MM}$ CSA tensor calculations, it is important to evaluate whether the number of MD frames and the sampling intervals, which are required to accurately represent the accessible conformational space for each residue, are sufficient. Such analysis was carried out for the highly mobile G89 and rigid E98 residues (Figure S7, Supporting Information). Interestingly, for both residues we find that averaging either 100 or 200 frames from a 100 ns


Figure 6. Left two panels: The plots of the amplitudes and orientations of the backbone ${ }^{15} \mathrm{~N}^{\mathrm{H}}$ CSA tensors in HIV-1 CA, in the molecular frame, calculated by $\mathrm{QM} / \mathrm{MM}$ (at the DFT level) for the starting structure (left) and averaged along the MD trajectory (right). Right panel: probability distributions for Euler angles $\alpha$ (black), $\beta$ (blue), and $\gamma$ (red) over the course of the MD trajectory. The plots are shown for selected CA residues: (a) H84, (b) H87, (c) G89, (d) I91, (e) A92, and (f) E98.
trajectory ( 1 - or 0.5 -ns sampling interval, respectively) yields similar $\delta_{\sigma}$ values ( $\pm 2 \%$ ), essentially identical within experimental error. Averaging 100 frames from the first 10 ns of the

MD trajectory yields essentially identical $\delta_{\sigma}$ values for the static E98, while a difference of 5.4 ppm is observed for the dynamic G89. Therefore, it appears that longer MD trajectories are
required to reach more quantitative agreement with experiment.

To rule out that the details of the particular DFT methodology used in the current calculations for G89 biased the resulting CSA parameters, we applied three commonly used density functionals: B3LYP, OLYP, and O3LYP. All three yield $\delta_{\sigma}$ values to within $4 \%$, i.e. vary less than the difference between the experimental and the calculated values, confirming that all three functionals are indistinguishable in outcome (Figure S8, Supporting Information).

Overall, the differences observed here between computations and experiment for certain residues highlight the importance of long trajectories and the development of MD protocols that enhance sampling of biologically relevant states. With computational cost decreasing rapidly, they should no longer be an impediment to calculate dynamically averaged CSA calculations by quantum mechanical methods. Such calculations are feasible and represent the method of choice for a rigorous analysis of the structural vs dynamic contributions to chemical shifts, as demonstrated here.

## - CONCLUSIONS AND FUTURE OUTLOOK

Residue-specific ${ }^{15} \mathrm{~N},{ }^{13} \mathrm{C}$, and ${ }^{1} \mathrm{H}$ CSA tensors are readily accessible using contemporary multidimensional RNCSA methods, ${ }^{15,16,29}$ even for large protein assemblies. These experiments provide uniquely rich information about the geometry, electronic structure, and dynamics. ${ }^{15} \mathrm{~N}$ CSA tensors provide a direct and sensitive probe of internal residue backbone dynamics occurring on time scales of nano- to microseconds. For tubular assemblies of the HIV-1 CA protein, investigated here, residues in the mobile CypA-binding loop exhibit dramatic decreases in ${ }^{15} \mathrm{~N}$ chemical shift anisotropy. The reduced anisotropy parameters, $\delta_{\sigma}$, unequivocally report on the presence of motions, unlike isotropic chemical shifts, where dynamic effects are not immediately obvious. Knowledge of dynamic regions in proteins and assemblies thereof is invaluable for accurate interpretation of chemical shifts in terms of geometric structure. The integrated analysis of combined experimental MAS NMR data, MD simulations, as well as QM methods for calculating chemical shifts in proteins using density functional theory provides rich and in-depth atomiclevel information on the inter-relatedness of internal motions and local structure. Here we show that the dynamic averaging of the CSA parameters results from Euler angle changes rather than variations in the principal components of the CSA tensor. This finding has important implications for the analysis of dynamics by solution NMR relaxation methods, where the shift anisotropy is taken as a constant. ${ }^{30}$ The integrated MAS NMR and MD/DFT approach developed and illustrated here is a powerful tool for atomic-resolution characterization of the structure and dynamics of biological assemblies.

## - MATERIALS AND METHODS

Protein Expression, Purification, and NMR Sample Preparation were performed as described previously. ${ }^{31}$ CA was expressed in E. coli Rosetta 2 (DE3), cultured in Luria-Bertani or modified minimal media, after induction with 0.4 mM IPTG at $23{ }^{\circ} \mathrm{C}$ for 16 h . The purification was performed with cation exchange column chromatography with $0-1 \mathrm{M} \mathrm{NaCl}$ gradient in a buffer containing 25 mM sodium phosphate $\mathrm{pH} 5.8,1 \mathrm{mM}$ DTT, and $0.02 \% \mathrm{NaN}_{3}$. Uniform ${ }^{15} \mathrm{~N}$ - and ${ }^{13} \mathrm{C}$-labeling was performed using ${ }^{15} \mathrm{NH}_{4} \mathrm{Cl}$ and ${ }^{13} \mathrm{C}_{6}$-glucose as sole nitrogen and carbon sources. Tubular assemblies of CA protein were prepared from $30 \mathrm{mg} / \mathrm{mL}$ protein solution in 25 mM phosphate buffer ( pH 5.5 ) containing 1 M NaCl . The solution was incubated at
$37{ }^{\circ} \mathrm{C}$ for 1 h and stored at $4{ }^{\circ} \mathrm{C}$ for subsequent NMR experiments. The incubated CA sample was pelleted by centrifugation at 6000 G for 15 min , the supernatant was removed, and $15 \mathrm{mg}(0.59 \mathrm{mmol})$ of fulllength tubular WT CA assemblies were packed into a Varian 3.2 mm MAS rotor. The rotor was sealed using an upper spacer and a top spinner.
MAS NMR Experiments were carried out on a 21.1 T ultrawide bore spectrometer outfitted with a 3.2 mm HXY Enhanced-Design Low-E MAS probe designed and built at NHMFL. ${ }^{32}$ Larmor frequencies were 899.1 MHz $\left({ }^{1} \mathrm{H}\right)$, 226.1 $\mathrm{MHz}\left({ }^{13} \mathrm{C}\right)$, and $91.1 \mathrm{MHz}\left({ }^{15} \mathrm{~N}\right)$. The MAS frequency was set at 14 kHz for all experiments, and was controlled to within $\pm 5 \mathrm{~Hz}$ by a Bruker MAS controller. KBr was used as temperature sensor, and the actual temperature of the sample was maintained to within $4 \pm 0.1{ }^{\circ} \mathrm{C}$ using the Bruker temperature controller. ${ }^{13} \mathrm{C}$ and ${ }^{15} \mathrm{~N}$ chemical shifts were referenced with respect to the external standards adamantane and $\mathrm{NH}_{4} \mathrm{Cl}$, respectively. In the ${ }^{15} \mathrm{~N}$ RNCSA 3D experiment, the typical $90^{\circ}$ pulse lengths were $2.5 \mu \mathrm{~s}$ $\left({ }^{1} \mathrm{H}\right), 3 \mu \mathrm{~s}\left({ }^{13} \mathrm{C}\right)$, and $5 \mu \mathrm{~s}\left({ }^{15} \mathrm{~N}\right)$, and the contact time of ${ }^{1} \mathrm{H}-{ }^{15} \mathrm{~N}$ cross-polarization (CP) was $1.0 \mathrm{~ms} .{ }^{1} \mathrm{H}-{ }^{15} \mathrm{~N}$ CP employed a linear amplitude ramp on the ${ }^{1} \mathrm{H}$ channel with the center Hartmann-Hahn matched to the first spinning sideband. The band-selective magnetization transfer from ${ }^{15} \mathrm{~N}$ to ${ }^{13} \mathrm{C}^{\alpha}$ was realized through a 4.5 ms SPECIFIC-CP with a tangent amplitude ramp on the ${ }^{15} \mathrm{~N}$ channel (49 kHz rf field center) and a constant rf field on the ${ }^{13} \mathrm{C}$ channel (35 kHz ). High-power ${ }^{1} \mathrm{H}$ continuous wave (CW) decoupling ( 110 kHz ) was applied during the SPECIFIC-CP period, and SPINAL-64 decoupling ( 100 kHz ) was applied during the direct $\left(t_{3}\right)$ and indirect $\left(t_{2}\right)$ acquisition periods. A R14 ${ }_{2}{ }^{5}$-based symmetry sequence was used to reintroduce ${ }^{15} \mathrm{~N}$ CSA interaction during the $t_{1}$ evolution period, and the phase-alternated $\left( \pm 5 \pi / 14\right.$ or $\left.\pm 64.29^{\circ}\right)$ rf field irradiation ( 49 kHz ) was applied on the ${ }^{15} \mathrm{~N}$ channel. Simultaneous $\pi$ pulses were applied on the ${ }^{13} \mathrm{C}$ channel at the center of every two rotor periods to decouple ${ }^{15} \mathrm{~N}-{ }^{13} \mathrm{C}$ dipolar interactions, and ${ }^{1} \mathrm{H} \mathrm{CW}$ was applied to decouple ${ }^{1} \mathrm{H}-{ }^{15} \mathrm{~N}$ dipolar interactions.
Numerical Simulations of ${ }^{15} \mathrm{~N}$ RNCSA line shapes were performed with the SIMPSON software package, ${ }^{33}$ versions 2.0 . To produce a powder average, 320 pairs of $\{\alpha, \beta\}$ angles generated according to the REPULSION algorithm and $16 \gamma$ angles (resulting in a total of 5120 angle triplets) were used for all simulations. The Haberlen-MehringSpiess convention was followed to define the CSA parameters in the present work, where the isotropic chemical shift $\delta_{\text {iso }}$, the reduced anisotropic chemical shift $\delta \sigma$, and the asymmetry parameter $\eta$ are related to the principal elements $\delta_{i i}(i=1,2$, or 3$)$ of the chemical shift tensor according to $\left|\delta_{11}-\delta_{i s o}\right| \geq\left|\delta_{33}-\delta_{\text {iso }}\right| \geq\left|\delta_{22}-\delta_{\text {iso }}\right|$, $\delta_{i s o}=1 / 3\left(\delta_{11}\right.$ $\left.+\delta_{22}+\delta_{33}\right), \delta_{\sigma}=\delta_{11}-\delta_{i s o}$, and $\eta=\left(\delta_{22}-\delta_{33}\right) /\left(\delta_{11}-\delta_{i s o}\right)$. For extracting the best-fit ${ }^{15} \mathrm{~N}$ CSA NMR parameters $\left(\delta_{\sigma}, \eta\right)$, all of the experimental and processing parameters (i.e., Larmor frequency, MAS frequency, RF field strength, number of $t_{1}$ points, finite pulse lengths, zero-filling, line broadening, etc.) were taken into account in the simulations. With the attainable sensitivity and resolution, a total of 76 nonoverlapping ${ }^{15} \mathrm{~N}$ CSA line shapes were extracted and fitted.
Molecular Dynamics Simulations of the wild type CA monomer (HXB2 polymorph, PDB ID 3NTE) were performed using ACEMD as reported previously. ${ }^{10}$ Ions in close proximity to the protein were placed using the CIONIZE routine in VMD; bulk waters and $\mathrm{Na} / \mathrm{Cl}$ ions were then added using VMD, ${ }^{34,35}$ setting the total concentration of NaCl to 1 M . The system was then equilibrated using NAMD 2.9 with the CHARMM36FF at 300 K for 100 ns .
QM/MM Calculations of Magnetic Shielding Anisotropy Tensors were carried out in Gaussian09, ${ }^{36}$ and an automated fragmentation quantum mechanics/molecular mechanics approach (AF-QM/MM) from the AFNMR package ${ }^{25}$ of ShiftS was used to divide the entire protein system into nonoverlapping fragments, in which the QM region included a fragment within 4 or $3 \AA$ from the target residue (without or with protons included, respectively). The MM region included the rest of the residues beyond the core and the buffer regions. AF-QM/MM was performed to generate an individual spin system for each target residue. In this work, the DFT calculations of the NMR calculations were performed by the GIAO method using the OLYP density functional and the TZVP basis set, and all of the
calculated ${ }^{15} \mathrm{~N}$ magnetic shieldings were referenced to the isotropic shielding constant of 237.8 ppm , as reported previously for the computations at the same level of theory in Ubiquitin (PDB ID: 1D3Z); the calculated 13C magnetic shieldings were referenced to the isotropic shielding constant of 190.8 ppm , according to the RMSDbased referencing method. ${ }^{37}$
Averaged Chemical Shift Tensor Calculations were performed by combining $\mathrm{QM} / \mathrm{MM}$ calculations with MD simulations. A total of 100 frames were extracted from the first 10 ns from the 100 ns MD trajectory. For each frame, the AF-QM/MM was performed to generate an individual spin system for each target residue. For each target residue, we performed the $100 \mathrm{QM} / \mathrm{MM}$ calculations using Gaussion09, and the backbone ${ }^{15} \mathrm{~N}$ chemical shielding tensors for the target residue were extracted from each calculation, as follows:

$$
\boldsymbol{\sigma}^{i}=\left[\begin{array}{ccc}
\sigma_{x x}^{i} & \sigma_{x y}^{i} & \sigma_{x z}^{i}  \tag{1}\\
\sigma_{y x}^{i} & \sigma_{y y}^{i} & \sigma_{y z}^{i} \\
\sigma_{z x}^{i} & \sigma_{z y}^{i} & \sigma_{z z}^{i}
\end{array}\right]
$$

where $i$ denotes the index of the frame extracted from the MD trajectory.

The magnetic shielding anisotropy tensor is expressed in its principal axes system (PAS) as

$$
\boldsymbol{\Lambda}^{i}=\left[\begin{array}{ccc}
\sigma_{11}^{i} & 0 & 0  \tag{2}\\
0 & \sigma_{22}^{i} & 0 \\
0 & 0 & \sigma_{33}^{i}
\end{array}\right]
$$

The dynamically averaged ${ }^{15} \mathrm{~N}$ chemical shielding tensor for each residue was then obtained by linear averaging of its nine elements extracted from the QM/MM calculations for each of the 100 individual substructures in the MD trajectory,

$$
\langle\boldsymbol{\sigma}\rangle=\frac{1}{N} \cdot\left[\begin{array}{lll}
\sum_{i=1}^{N} \sigma_{x x}^{i} & \sum_{i=1}^{N} \sigma_{x y}^{i} & \sum_{i=1}^{N} \sigma_{x z}^{i}  \tag{3}\\
\sum_{i=1}^{N} \sigma_{y x}^{i} & \sum_{i=1}^{N} \sigma_{y y}^{i} & \sum_{i=1}^{N} \sigma_{y z}^{i} \\
\sum_{i=1}^{N} \sigma_{z x}^{i} & \sum_{i=1}^{N} \sigma_{z y}^{i} & \sum_{i=1}^{N} \sigma_{z z}^{i}
\end{array}\right]
$$

where $N$ denotes the number of total frames taken for QM/MM calculations for the residue of interest; in the present work $N=100$. The averaged ${ }^{15} \mathrm{~N}$ chemical shielding tensors were referenced to the isotropic shielding constant of 237.8 ppm to obtain the motionaveraged chemical shift tensor, $\langle\boldsymbol{\delta}\rangle$, and the principal components, $\delta_{i j}$ for each target residue.

To obtain the time-dependent orientation of the chemical shielding tensors in the laboratory frame, for each target residue, rotations in Cartesian space were used to express the orientation relative to the stationary set of axes in each frame. These were parametrized by three Euler angles $\alpha, \beta$, and $\gamma$, according to the standard notation: ${ }^{38}$

$$
\begin{equation*}
\boldsymbol{\sigma}^{i}=\mathbf{R}^{i} \cdot \Lambda^{i} \cdot\left(\mathbf{R}^{i}\right)^{-1} \tag{4}
\end{equation*}
$$

where $\mathbf{R}$ denotes the corresponding rotation matrix, expressed as

$$
\mathbf{R}=\left[\begin{array}{ccc}
\cos \alpha \cos \beta \cos \gamma & \sin \alpha \cos \beta \cos \gamma & -\sin \beta \cos \gamma  \tag{5}\\
-\sin \alpha \sin \gamma & +\cos \alpha \sin \gamma & \\
-\cos \alpha \cos \beta \sin \gamma & -\sin \alpha \cos \beta \sin \gamma & \sin \beta \sin \gamma \\
-\sin \alpha \cos \gamma & +\cos \alpha \cos \gamma & \\
\cos \alpha \sin \beta & \sin \alpha \sin \beta & \cos \beta
\end{array}\right]
$$

Chemical shift prediction ShiftX was also used to calculate the dynamically averaged ${ }^{15} \mathrm{~N}$ isotropic chemical shifts for the individual 5000 frames during the 100 ns MD trajectory.

## ASSOCIATED CONTENT

## (5) Supporting Information

The Supporting Information is available free of charge on the ACS Publications website at DOI: $10.1021 /$ jacs. 6 b 08744.

Experimental and simulated ${ }^{15} \mathrm{~N}$ CSA line shapes; distribution plots for isotropic chemical shifts; principal components of the ${ }^{15} \mathrm{~N}$ CSA tensor for selected CA residues; simulated rigid and motionally reduced ${ }^{15} \mathrm{~N}$ CSA line shapes; individual components of the ${ }^{15} \mathrm{~N}$ CSA tensor for selected CA residues; probability distribution plots of ${ }^{15} \mathrm{~N}$ isotropic chemical shifts calculated by Shiftx based on MD simulation; Euler angles of the ${ }^{15} \mathrm{~N}$ CSA tensors for the G89 and E98 residues of CA calculated from MD/DFT with different sampling schedules and with different functionals (PDF)

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## Author Contributions

"H.Z. and G.H. have contributed equally

## Notes

The authors declare no competing financial interest.

## ACKNOWLEDGMENTS

This article is dedicated to the memory of Professor Oleg Jardetzky. This work was supported by the National Institutes of Health (NIH Grants P50 GM082251, P41 GM104601, and P50 GM103297 from NIGMS). We acknowledge the support of the National Science Foundation (NSF Grant CHE0959496) for the acquisition of the 850 MHz NMR spectrometer at the University of Delaware and of the National Institutes of Health (NIH Grants P30GM103519 and P30GM110758) for the support of the core instrumentation infrastructure at the University of Delaware. This research is part of the Blue Waters sustained-petascale computing project supported by NSF (PRAC Award ACI-1440026). A portion of this work was performed at the National High Magnetic Field Laboratory, which is supported by National Science Foundation Cooperative Agreement No. DMR-1157490 and the State of Florida.

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[^0]:    Received: August 21, 2016
    Published: October 5, 2016

